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| Realization of a perceptron in VHDL |
| Project for the exam of Digital System of prof. Fanucci |
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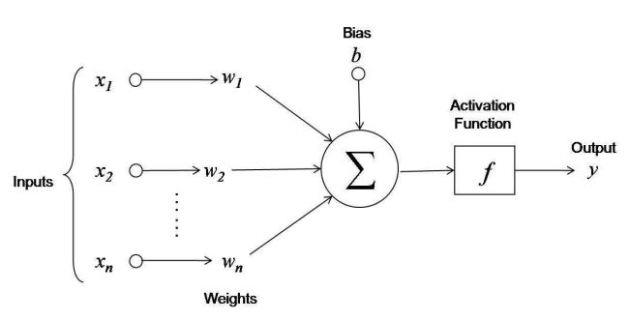
# Goal of the project

The project aims to realize a single perceptron in VHDL and make an implementation for a Zynq-7000 FPGA using the Vivado tool and analyze that implementation.

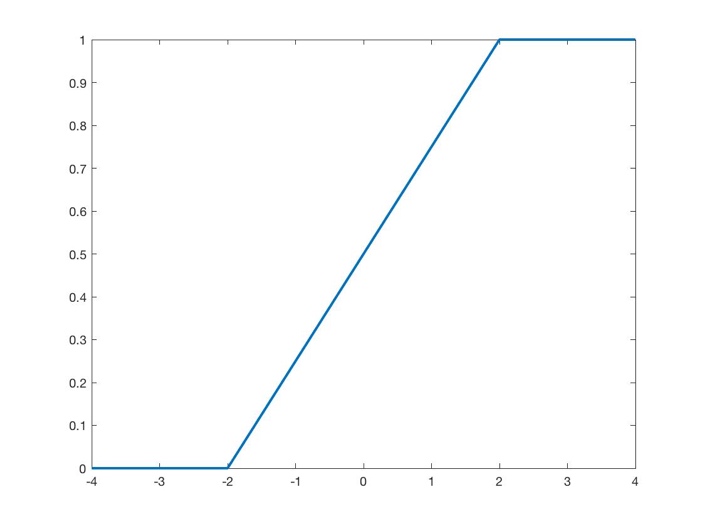
# Specifications

The perceptron network takes inputs represented using bits. The network multiplies each input with a coefficient and adds all of the results with a bias .

and are represented using bits. , and are in the range [-1; 1].



The result of this sum is given as input to an activation function which tf is graphed below:



The output of this function is given as system output and is represented by using bits.

# Matlab model

To have a comparison with the results of the testbench I realized a Matlab model of the activation function (file activation.m) and of the whole perceptron (file perceptron.m). I’ve then realized a test to check that the realized model fits the specification (file perceptron\_test.m).

I’ve defined as the output of the sum of all of the products with the bias and I’ve passed it as input to the activation function.

To build the activation function I’ve divided it into three different regions:

1. ;
2. ;

# Digital representation

To represent values in digital domain I choose to use fixed point representation, so I have to compute LSB to convert real values into discretized domain.

;

To do product there is no need to align LSB so we can compute:

bits and have

To get we have to sum 11 terms, ten of which have the same number of bits (only bias have fewer bits) so the number of bits needed to represent sum output is:

bits

Consider now just the sum between products results: all of these values have the same LSB so no alignment is required. To sum the bias instead we need to align LSB:

while

So before to sum bias I have to add zeroes bits at right of bias, then I need to add further bits at left of bias by replicating the MSB (which is the sign).

After this sum the activation function will receive as input a 21 bits value representing , this value have to be compared with 2 and -2 to determine in which of the three regions of the activation function we are. To achieve this goal is needed to compute the representation of these two values in digital domain:

and

Then I have to compute the values for the output of the activation function, I compute these values with the precision allowed by the sum output (so 21 bits) and then I’ll truncate to fit in y:

When implementing in VHDL I’ve further converted these values into binary representation. To perform the division by four for the linear part formula I’ve done two right shifts of .

All of these computations can also be found on the attached file *bits\_counts.m*

# VHDL implementation

With all of the previous considerations I’ve wrote the VHDL code to implement the system:

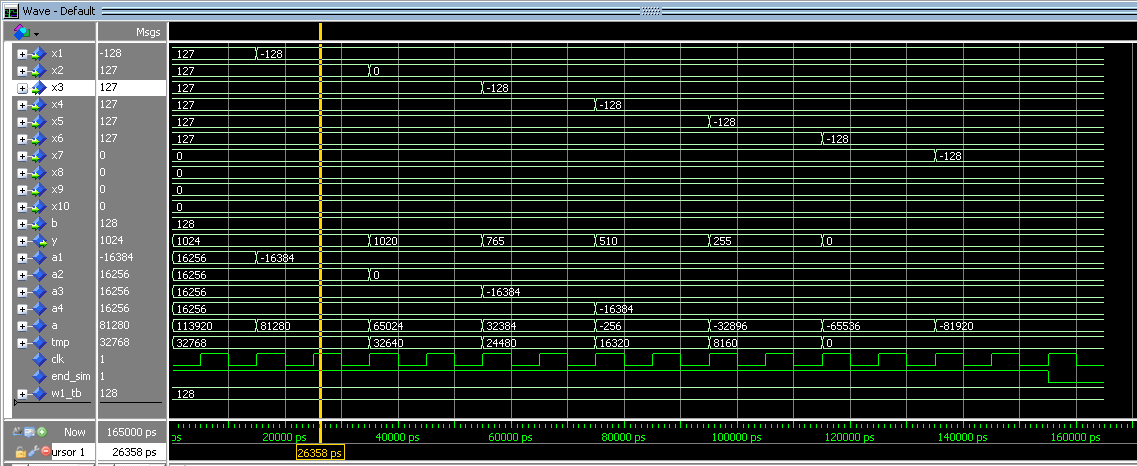
* perceptron.vhd – contains the implementation of the simple perceptron
* perceptron\_tb.vhd – testbench for the perceptron implementation above
* perceptron\_wrapper.vhd – wrapper adding two flip flops one at the perceptron input and one to the perceptron output to make the system synchronous
* perceptron\_wrapper\_zybo.vhd – wrapper used to adapt the system for an implementation into a Zybo board: the only inputs becomes x, while the w and b are stucked at 0.5 (010000000). As the previous wrapper it have two flip flops: one at the input of the perceptron and one at the output to make system synchronous
* flip\_flop\_n\_bit.vhd – flip flop used in the wrapper
* perceptron\_wrapper\_tb.vhd – testbench for the perceptron\_wrapper\_zybo implementation

All of these files are attached to this paper and are divided in two folders contained into vhd folder: tb (contains only the testbench) and src (contains all of the other files).

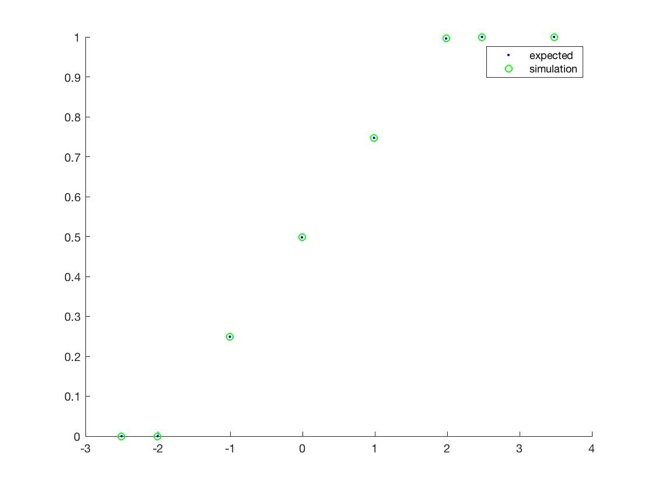
# Testbench verification in Modelsim

To verify the correctness of the implementation I checked the behavior of the system in with eight different inputs. These inputs are chosen in order to verify the behavior of the activation function in all of the three regions. For simplicity I have chosen to use just the first seven inputs and set all weights and bias to the same value of 0.5. The testbench verification has been done directly on the perceptron model without any wrapper.

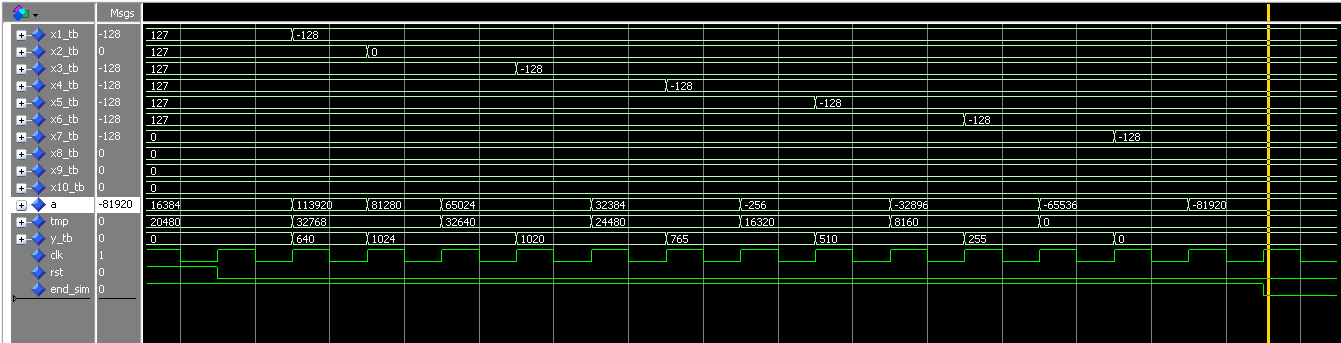
The check is done by comparing the values of with the ones computed in Matlab, then the same is done with and the output of the activation function in Matlab. The comparison is performed with instead that with because is not truncated and so the two values should perfectly overlap.

The picture below shows the results of running the testbench on Modelsim:

This other picture below shows the comparison between the results of simulation and expected ones, how is possible to see they perfectly overlaps:



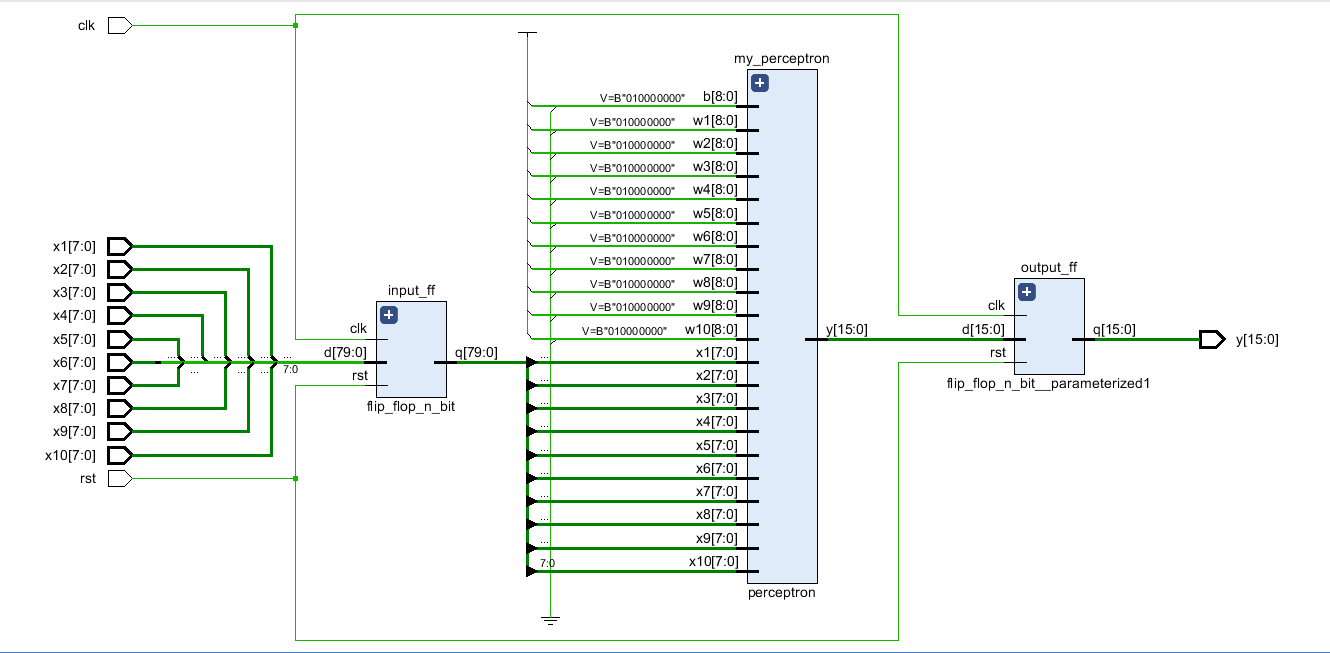
The same procedure is done with the testbench made for the perceptron\_wrapper\_zybo and as we can see from the testbench simulation below the results are the same as expected:



# Vivado synthesis and implementation

After verification the VHDL code of the system has been imported into Vivado tool to make synthesis and implementation for a Zybo Board.

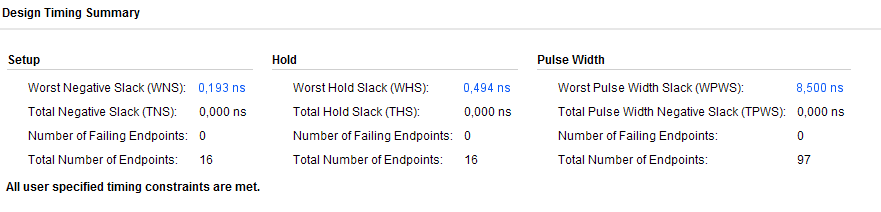
First I ran the RTL elaboration to compile the code and check that the schematic is correct, here is the schematic of the perceptron with the wrapper for the Zybo board:



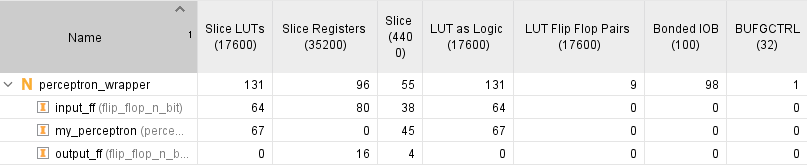
After running synthesis without any constraints to check for any error I selected 10 ns of clock period to analyze the slack and consequently adjust the clock frequency: there were a worst negative slack of about 7 ns so I choosed to increase clock period to 18 ns in order to have also a little of margin for further steps because at synthesis phase the program does not consider delay due to routing.

After that I mapped all input and outputs to package pins. Because the Zybo board have only 100 I/O pins in the wrapper I have had to reduce the number of inputs by making all weights and the bias get stuck at 0.5 and having as only inputs just the x, rst and clk and as output y, this way are used 98 out of the 100 pins available. Once mapped all signals to pins I ran again the synthesis to check for correctness in pins assignment and to verify again that the timing constraints are meet.

After running implementation stage the program gave no errors and I checked again that timing constraints are met (see picture below).



The final implementation made by Vivado just signals one warning which is due to the fact that the Arm processor which is present on the board is not used, but it’s fine. In the picture below we can see the cells of the FPGA that are needed by the system:



# Timing and power considerations

The slack time is defined as:

and depends on the logic and technology used while depends on the design. So the only thing that we can directly adjust without changing technology or design is the clock period:

So if we want to have the theoretical maximum clock frequency allowed without having a timing violation we have to set . As we have seen the final worst negative slack computed is 0.193ns with a clock period of 18ns so theoretically the maximum clock frequency we can use is:

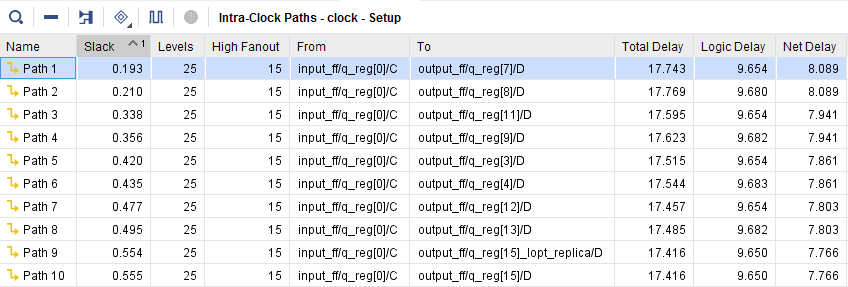
This result is just theoretical because we are not taking into account the delay due to routing which are known only when we will physically implement the logic on the FPGA.

So in the implementation I’ve left a clock period of 18ns in order to have a margin that would guarantee that even with the additional delay due to routing the system won’t have a setup violation.

Other possible solutions to increase clock frequency of our device could be:

* choose a different technology (changing so the FPGA used) to reduce and ; this will have a direct impact on costs because choosing a faster technology would be more expensive and could be not ever possible, for example in the choice of our FPGA we are also constrained by the number of I/O pins needed.
* pipeline the logic of the system by adding (for example) an additional flip flop just before the activation function. This way we will reduce the propagation delay of the critical path, so will reduce in spite of an increasing of the complexity of the system (additional logic is required so additional consumption).
* change the design to reduce the critical path delay; not easy.

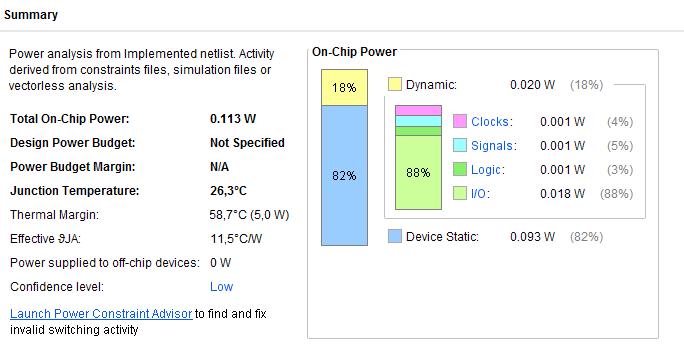
The critical path is computed by the Vivado tool and is the one that goes from the LSB of x1 to the 7th bit of the y as we can see from the picture below:



From the point of view of power consumption we have to remember that increasing the clock frequency will lead to an increase of the dynamic power consumption following the relation:

Moreover, as previously mentioned, if we increase the logic to pipeline the system we also have to take into account an increase of the capacitance of the system and so an increase of the dynamic power consumption.

The power consumption of the implemented system has been computed by Vivado and is:



# Possible applications

This system could be used in smart environment to give an hardware acceleration for computation of neural networks. For example in a smartphone could be embedded an FPGA programmable by the processor on the fly to set the proper weights and do the needed computation; this will allow to reduce the load for the processor increasing so the overall performance because this customized logic allows to obtain lower power consumption and faster computation in calculation of activation functions with respect to a CPU. Since iPhone 7, Apple started introducing low power FPGA into his devices to run machine learning algorithms.